

# Workshop on Three-Nucleon Interactions and Nuclear Dynamics

Beckmanns Hof, Ruhr University Bochum

Dec 8 – 12, 2025



# A bit of history...



Photo courtesy of Kimiko Sekiguchi

January 2025 at Tohoku University in Sendai





Ruhr University Bochum gets on Japanese TV...

## Bochum





# Workshop on Three-Nucleon Interactions and Nuclear Dynamics

	Monday	Tuesday	Wednesday	Thursday	Friday
9:30 am	Talks	Talks	Talks	Talks	Talks
noon	Lunch	Lunch	Lunch	Lunch	Lunch
2:00 pm	Talks	Free discussions	Free discussions	Talks	
5:00 pm					

- Talks are for 20 + 5 or 40 + 10 min
- **Feel free to ask questions during the talks!**
- We plan to post talks online (upon your permission)
- For discussions, you can use this room (available till 5pm) or office space at TP2
- Coffee breaks are taken in a separate room (called „Tours“)

# Workshop on Three-Nucleon Interactions and Nuclear Dynamics

	Monday	Tuesday	Wednesday	Thursday	Friday
9:30 am	Talks	Talks	Talks	Talks	Talks
noon	Welcome lunch	Lunch	Lunch	Lunch	Lunch
2:00 pm	Talks	Free discussions	Free discussions	Talks	
5:00 pm	Christmas market in Bochum		Dinner together in Dortmund + Opera Turandot	Workshop dinner	



# Organizational remarks

For dinner, you can find a plenty of restaurants in the Bochum downtown area, e.g. around Bermuda3eck

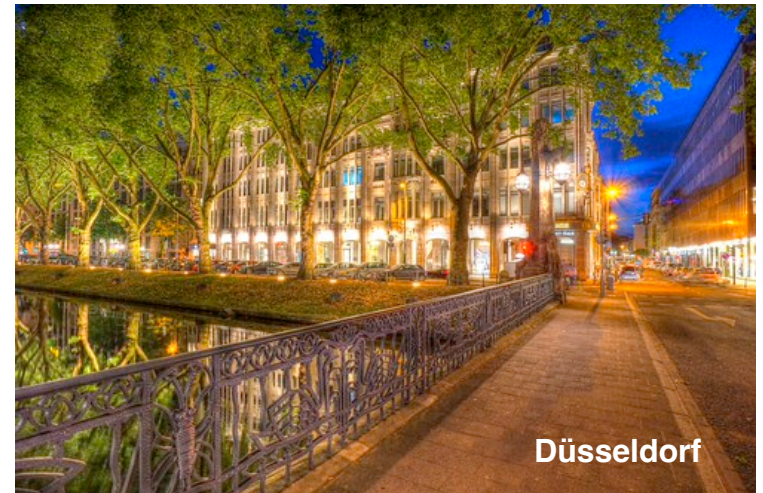


Some inspiration for free time:



Hattingen

- a small village near Bochum with a nice old town (half-timbered houses)
- easily reachable from Bochum via tram U308
- has a nice Christmas market



Düsseldorf

- takes about 40 min by train from Bochum HbF

# Traveling recommendations



Plan sufficient time for your travel (especially on the way to the airport!)

Use the app DB Navigator (allows to buy tickets and provides information on delays)

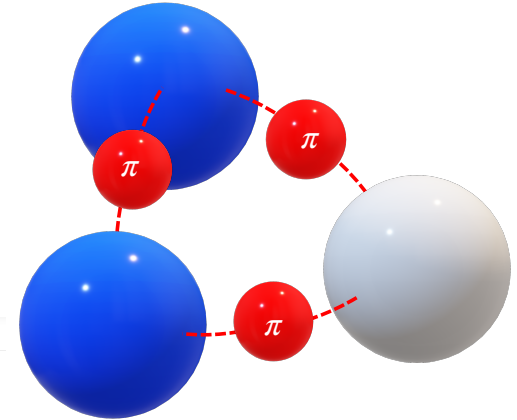
Alternatively, use [this page](#) to get information about delays





# Workshop on Three-Nucleon Interactions and Nuclear Dynamics

— scientific introduction —



JUNE 15, 1939

PHYSICAL REVIEW

## Many-Body Interactions in Atomic and Nuclear Systems

H. PRIMAKOFF, *Polytechnic Institute of Brooklyn, Brooklyn, New York*

AND

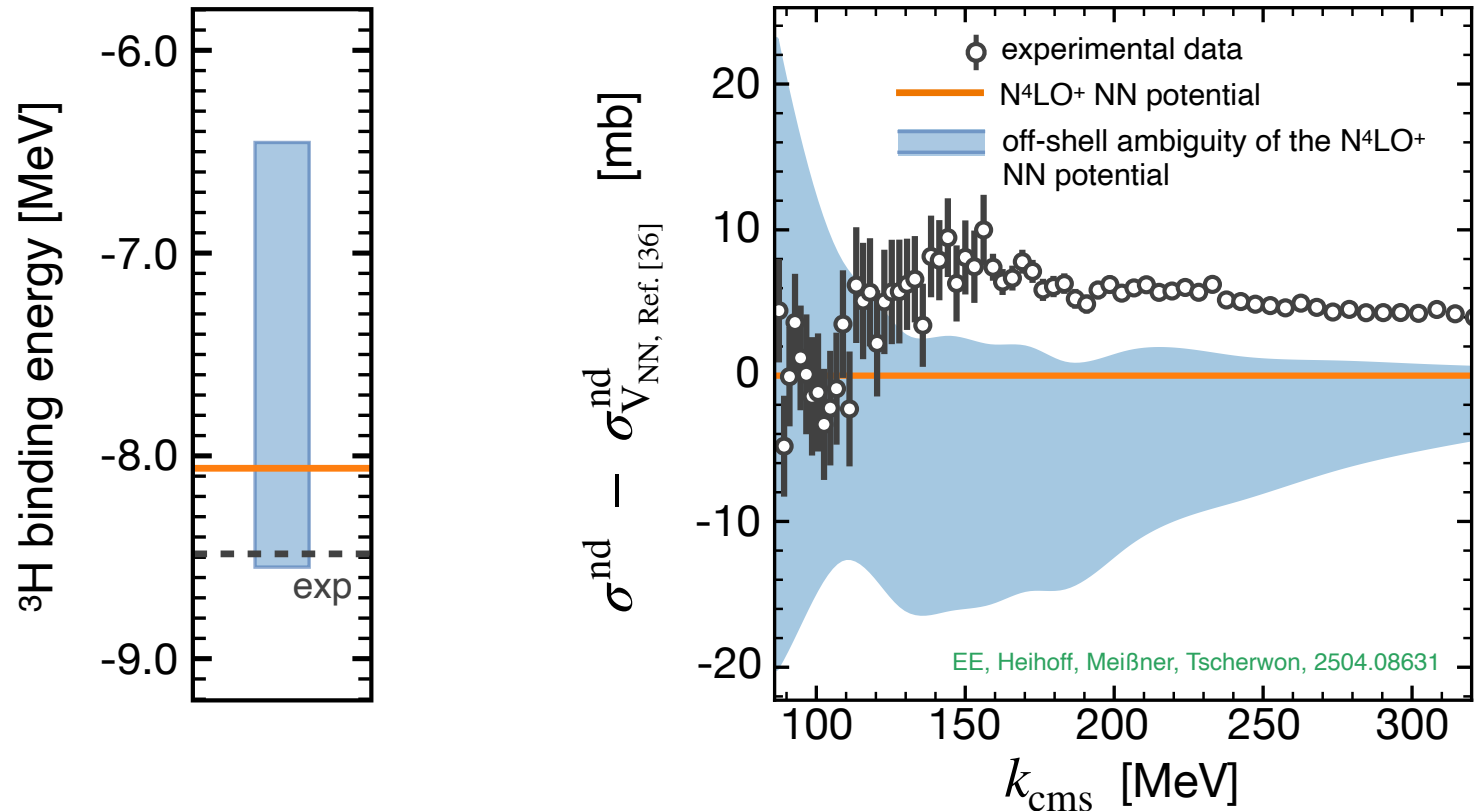
T. HOLSTEIN,\* *New York University, University Heights, New York, New York*

(Received March 28, 1938)

When particles interact with each other through the intervening mechanism of a field, the description of their dynamical behavior by means of action-at-a-distance potentials is only of an approximate nature. Two-body, three-body, ...,  $m$ -body potentials may be regarded as successive stages of this approximation; their relative magnitudes are examined systematically for several types of classical and quantized fields, e.g., electromagnetic, mesotron, etc. It is found that the description of electrons

in atomic systems by the customary two-body potentials is an excellent approximation; in nuclei, independent of the details of the field, one finds: three-body potentials  $\cong (v_n/c) \times (\text{two-body potentials}) \cdots$ ,  $m$ -body potentials  $\cong (v_n/c)^{m-2} \times (\text{two-body potentials})$ , where  $v_n$  is the average velocity of the heavy particles in the nucleus. The usual description of nuclei in terms of two-body potentials cannot therefore be considered satisfactory, except in the case of the deuteron.

# 3NF effects in the 3N system



- 3NFs are small (but important) corrections to the NN interactions
- 3NFs depend on the (ambiguous) off-shell behavior of NN interactions [Polyzou, Glöckle '90](#)
- Large discrepancies in Nd scattering [\[talk by Kimiko\]](#); **no existing 3NF model is capable of improving (globally) the description of Nd data** [Kalantar-Nayestanaki, EE, Messchendorp, Nogga '12](#)

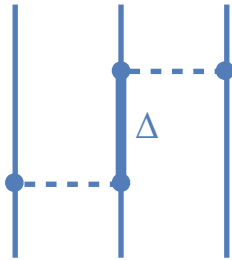


# Three-body force: A frontier in nuclear physics

Endo, EE, Naidon, Nishida, Sekiguchi, Takahashi, EPJA 61 (2025) 9

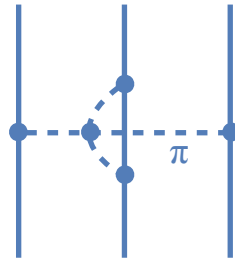
- Three-nucleon forces (3NF) are small **but important** corrections to the dominant NN forces

- 3NF mechanisms:

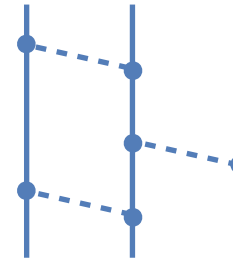


intermediate  $\Delta$ -excitation

Fujita, Miyazawa '57

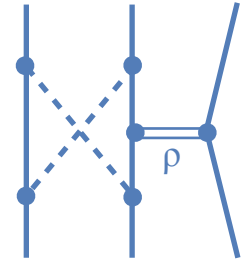


multi-pion interactions



off-shell behavior of the  $V_{NN}$

$$V_{\text{ring}} = \mathcal{A}_{3\pi} - V_{\pi} G_0 V_{\pi} G_0 V_{\pi}$$



short-range

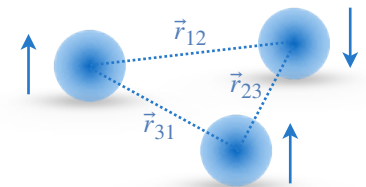
$\Rightarrow$  3NF are not directly measurable and depend on the scheme (DoF, off-shell  $V_{NN}$ , ...)

- 3NF have extremely rich and complex structure

— most general **local** 3NF: 
$$V_{3N} = \sum_{i=1}^{20} O_i f_i(r_{12}, r_{23}, r_{31}) + \text{permutations}$$

EE, Gasparyan, Krebs, Schat '15

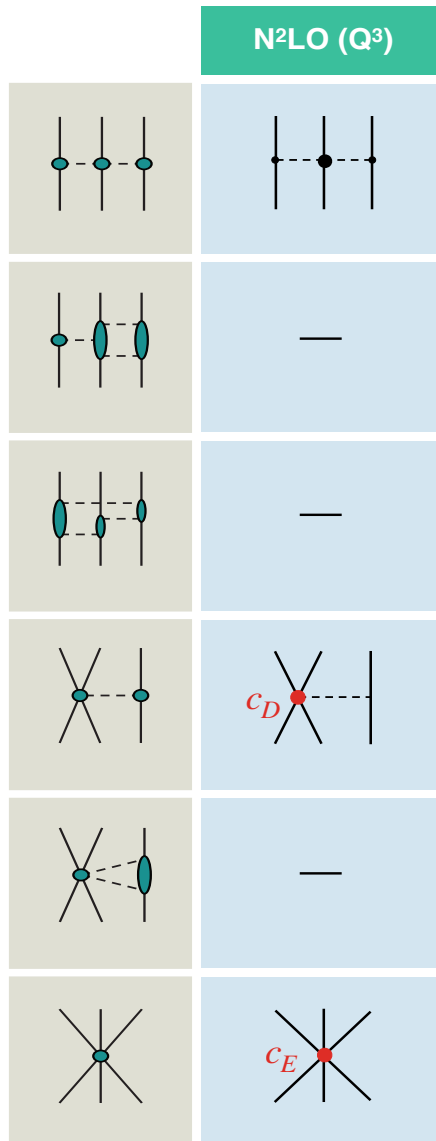
— most general **nonlocal** 3NF: **320 (!)** operators Topolnicki '17



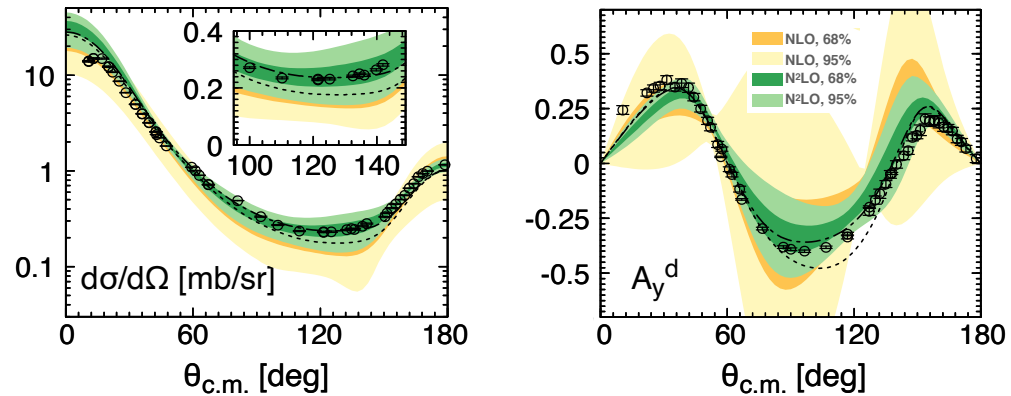
$\Rightarrow$  Guidance from theory indispensable — an opportunity for  $\chi$ EFT!

# Three-body force: A frontier in nuclear physics

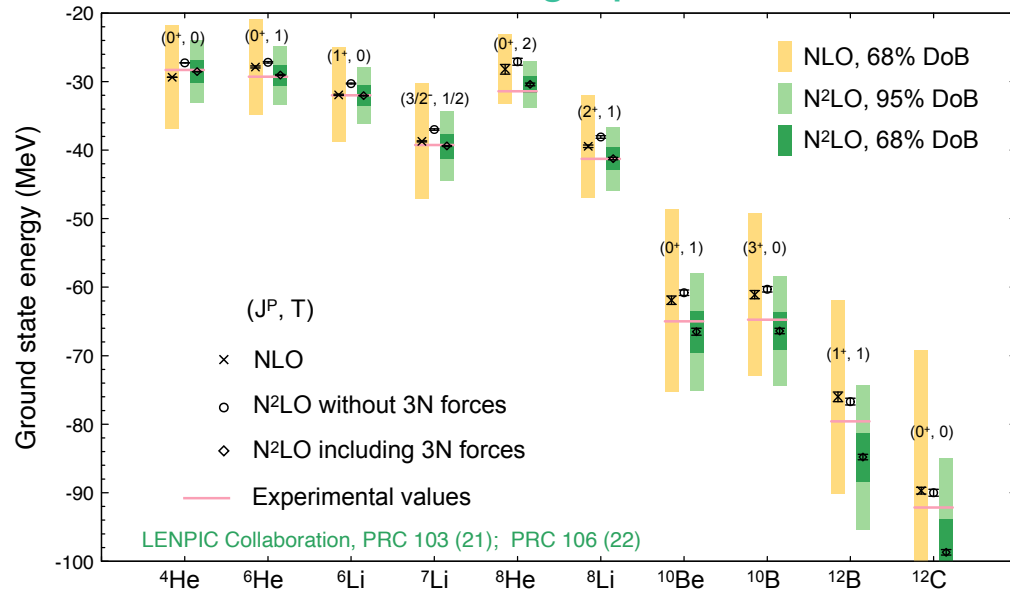
Endo, EE, Naidon, Nishida, Sekiguchi, Takahashi, EPJA 61 (2025) 9



Elastic Nd scattering at 135 MeV



Predictions for light p-shell nuclei



⇒ Guidance from theory indispensable — an opportunity for  $\chi$ EFT!



# Three-body force: A frontier in nuclear physics

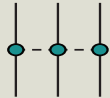
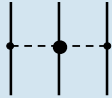


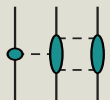


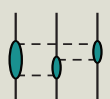


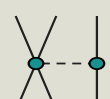



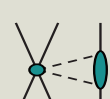




Endo, EE, Naidon, Nishida, Sekiguchi, Takahashi, EPJA 61 (2025) 9

	N <sup>2</sup> LO (Q <sup>3</sup> )	N <sup>3</sup> LO (Q <sup>4</sup> )	N <sup>4</sup> LO (Q <sup>5</sup> )
		 Ishikawa, Robilotta '08; Bernard, EE, Krebs, Meißner '08	 Krebs, Gasparyan, EE '12
	—	 Bernard, EE, Krebs, Meißner '08	 Krebs, Gasparyan, EE '13
	—	 Bernard, EE, Krebs, Meißner '08	 Krebs, Gasparyan, EE '13
		 Bernard, EE, Krebs, Meißner '11	 Krebs, Gasparyan, EE '13
	—	 Bernard, EE, Krebs, Meißner '11	 Krebs, Gasparyan, EE '13
		—	 13 LECs Girlanda, Kievski, Viviani '11

⇒ Guidance from theory indispensable — an opportunity for  $\chi$ EFT!

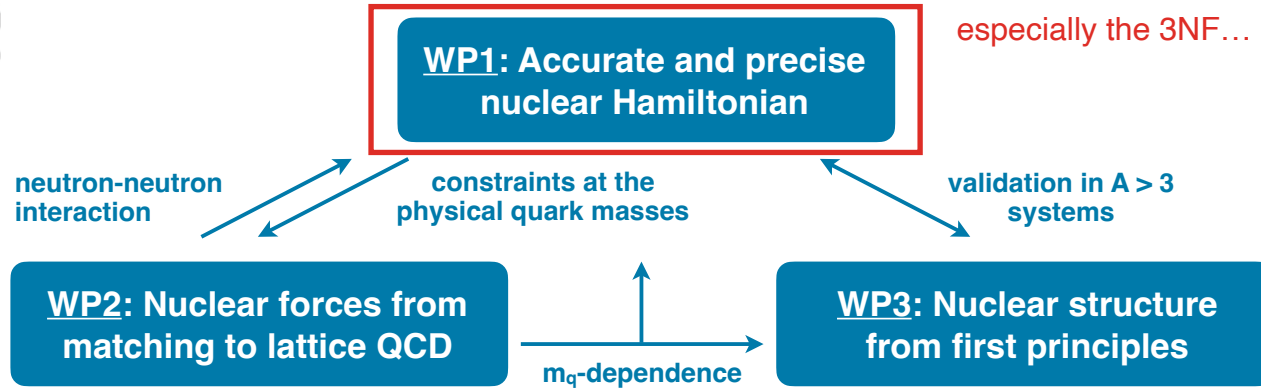
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	 $c_D$	 Bernard, EE, Krebs, Meißner '11	
	—	 Bernard, EE, Krebs, Meißner '11	
	 $c_E$	<p>mixing DimReg with Cutoff regularization in the Schrödinger equation violates <math>\chi</math>-symmetry  <math>\Rightarrow</math> need to be re-derived using symmetry-preserving Cutoff regularization</p>	

$\Rightarrow$  Guidance from theory indispensable — an opportunity for  $\chi$ EFT!

# NUCLEAR THEORY FROM FIRST PRINCIPLES



## The three-nucleon-force team in Bochum:



PD Dr. Hermann Krebs



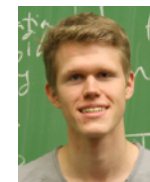
Dr. Arseniy Filin



Sven Heihoff



Josep Sola Cava



Patrick Walkowiak



Henri Huesmann



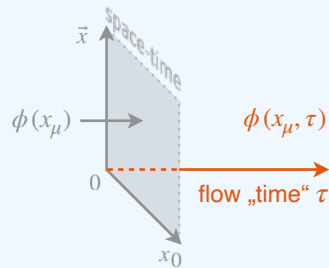
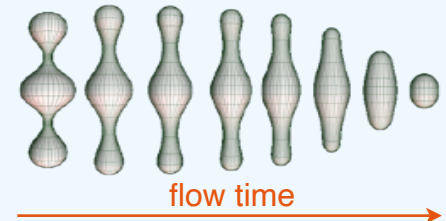
# Chiral gradient flow

Hermann Krebs, EE, PRC 110 (2024) 044003; PRC110 (2024) 044003

Gradient flows: methods for smoothing manifolds

(e.g., Ricci flow used in the proof of the Poincaré conjecture)

Gradient flow as a regulator in field theory



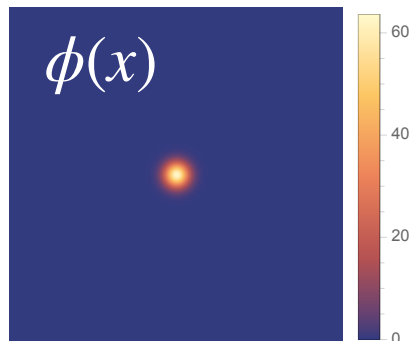
$$\text{Flow equation: } \frac{\partial}{\partial \tau} \phi(x, \tau) = - \left. \frac{\delta S[\phi]}{\delta \phi(x)} \right|_{\phi(x) \rightarrow \phi(x, \tau)}$$

subject to the boundary condition  $\phi(x, 0) = \phi(x)$

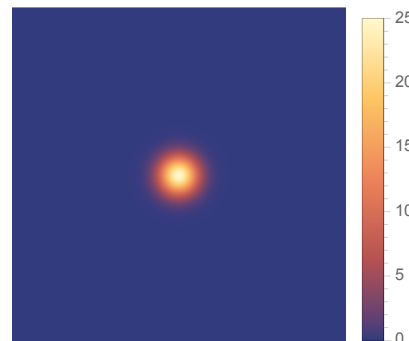
Free scalar field:

$$G(x, \tau) = \frac{\theta(\tau)}{16\pi^2 \tau^2} e^{-\frac{x^2 + 4M^2 \tau^2}{4\tau}}$$

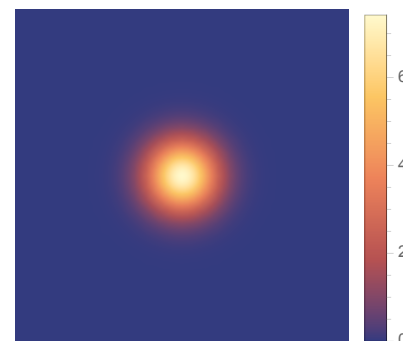
$$[\partial_\tau - (\partial_\mu^x \partial_\mu^x - M^2)] \phi(x, \tau) = 0 \quad \Rightarrow \quad \phi(x, \tau) = \int d^4 y \underbrace{G(x - y, \tau)}_{\text{heat kernel}} \phi(y) \quad \Rightarrow \quad \tilde{\phi}(q, \tau) = e^{-\tau(q^2 + M^2)} \tilde{\phi}(q)$$



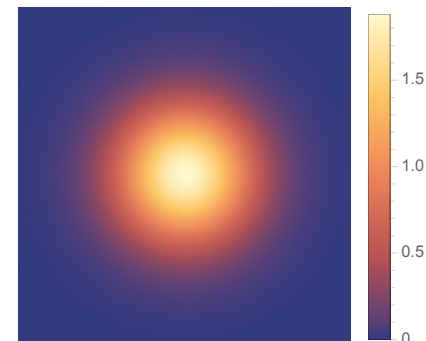
$\tau = 0$



$\tau = 1$



$\tau = 2$



$\tau = 4$

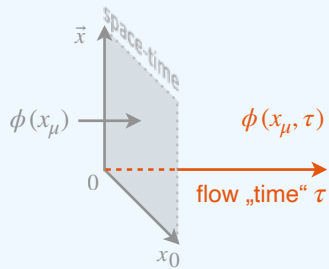
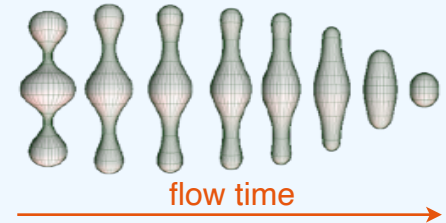
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Free scalar field:

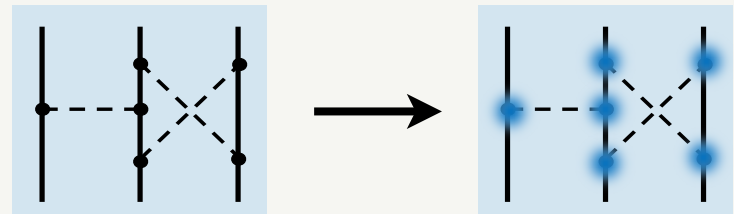
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YM gradient flow Narayanan, Neuberger '06, Lüscher, Weisz '11:  $\partial_\tau A_\mu(x, \tau) = D_\nu G_{\nu\mu}(x, \tau)$  ← extensively used in LQCD

Chiral gradient flow Hermann Krebs, EE, PRC 110 (2024) 044003  
PRC 110 (2024) 044004

Generalize  $U(x)$ ,  $U(x) \rightarrow RU(x)L^\dagger$  to  $W(x, \tau)$ :

$$\partial_\tau W = -i \underbrace{w^\dagger}_{\sqrt{W}} \text{EOM}(\tau) w, \quad W(x, 0) = U(x)$$



# Recent and ongoing activities

- ✓ Derivation of the  $N^3\text{LO}$  contributions to the 3NF using the GF method [Hermann](#)

(✓) Partial wave decomposition of the 3NF@ $N^3\text{LO}$   
[LENPIC](#) talk by Kai

- (✓) Re-determination of the  $\pi N$  LECs using the GF regulator [Patrick](#)

☑ Sensitivity studies of 3N scattering observables to the contact 3NF@ $N^4\text{LO}$  [Arseniy](#), [Josep](#), [Sven](#)

talks by Arseniy and Josep

- (✓) Sensitivity studies of 3N scattering observables to the off-shell LECs in the 2NF@ $N^3\text{LO}$  [Sven](#)

(✓) Derivation and implementation (partial wave decomposition) of  $c_D$ -like 3NF@ $N^4\text{LO}$  [Henri](#), [Hermann](#), [Arseniy](#)

talk by Henri

☑ Optimization/„emulation“ of 3N scattering calculations (needed to fix 3NF@ $N^4\text{LO}$ ) [Sven](#), [Arseniy](#)

✓ NN interactions „on demand“ (local LO, local+separable, low-resolution) [Sven](#)

(✓) Truncation uncertainty in chiral EFT via explicit marginalization over higher-order terms [Sven](#)

talk by Sven

☑ Chiral gradient flow: Chiral extrapolations, 3NF@ $N^4\text{LO}$ , 4NF, currents, ... [Hermann](#)

	Two-nucleon force	Three-nucleon force	Four-nucleon force
LO ( $Q^0$ )		—	—
NLO ( $Q^2$ )		—	—
$N^2\text{LO}$ ( $Q^3$ )			—
$N^3\text{LO}$ ( $Q^4$ )			
$N^4\text{LO}$ ( $Q^5$ )			—

# Enjoy the talks and discussions!